Pi: The Ultimate Ratio

Exploring the Ratio of Circle Circumference to Diameter

WARM UP

Scale up or down to determine an equivalent ratio.

1.
$$\frac{18 \text{ miles}}{3 \text{ hours}} = \frac{?}{1 \text{ hour}}$$

2.
$$\frac{\$750}{4 \text{ days}} = \frac{?}{1 \text{ day}}$$

3.
$$\frac{12 \text{ in.}}{1 \text{ ft}} = \frac{?}{5 \text{ ft}}$$

4.
$$\frac{48 \text{ oz}}{3 \text{ lb}} = \frac{?}{1 \text{ lb}}$$

LEARNING GOALS

- Identify pi (π) as the ratio of the circumference of a circle to its diameter.
- Construct circles using a compass and identify various parts of circles.
- Understand the formula for the circumference of a circle, and use the formula to solve problems.

KEY TERMS

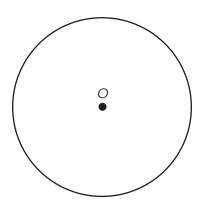
- congruent
- circle
- radius
- diameter
- circumference
- pi

You have learned about ratios. How can you use ratios to analyze the properties of geometric figures, such as circles?

Getting Started

Across and Around

A circle is shown with a point drawn at the center of the circle. The name of the point is O, so let's call this Circle O.



- Be sure to include units when you record your measurements.
- 1. Analyze the distance around the circle.
 - a. Use a string and a centimeter ruler to determine the distance around the circle.



b. How does your measurement compare to your classmates' measurements? Summarize the similarities and differences.



- a. Measure your line using your centimeter ruler.
- b. How does your measurement compare to your classmates' measurements? Summarize the similarities and differences.



Analyzing the Parts of a Circle



Everyone can identify a circle when they see it, but defining a circle is a bit harder. Can you define a circle without using the word round? Investigating how a circle is formed will help you mathematically define a circle.

Step 1: In the space provided, draw a point and label the point A.

1. Follow the given steps to investigate how a circle is formed.

Step 2: Use a centimeter ruler to locate and draw a second point that is exactly 5 cm from point A. Label this point B.

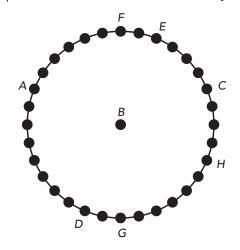
Step 3: Locate a third point that is exactly 5 cm from point A. Label this point C.

2. How many other points could be located exactly 5 cm from point A? How would you describe this collection of points in relation to point A?

Step 4: Repeat this process until you have drawn at least ten distinct points that are each exactly 5 cm from point A.

3. Define the term *circle* without using the word *round*.

A **circle** is a collection of points on the same plane equidistant from the same point. The center of a circle is the point from which all points on the circle are equidistant. Circles are named by their center point.



- 4. Use the circle shown to answer each question.
 - a. Name the circle.

The **radius** of a circle is a line segment formed by connecting a point on the circle and the center of the circle. The distance across a circle through the center is the diameter of the circle. The **diameter** of a circle is a line segment formed by connecting two points on the circle such that the line segment passes through the center point. The distance around a circle is called the **circumference** of the circle.

- b. Identify a radius of the circle.
- c. Identify a diameter of the circle.
- d. Are all radii of this circle the same length? Explain your reasoning.
- 5. What is the relationship between the length of a radius and the length of a diameter?





Measuring the Distance Around a Circle



Let's explore circles. Use circles A, B, D, E, and O provided at the end of the lesson. Circle O is the same as the circle from the activity Across and Around

1. Use a string and a centimeter ruler to measure the distance from a point on the circle to the center and the distance around each circle. Record your measurements in the table. In the last column, write the ratio of Circumference: Diameter in fractional form.

Circle	Circumference	Radius	Diameter	<u>Circumference</u> Diameter
Circle A				
Circle B				
Circle O				
Circle D				
Circle E				

- 2. Average the ratios recorded for $\frac{Circumference}{Diameter}$. What is the approximate ratio for the circumference to the diameter for the set of circles? Write the approximate ratio as a fraction and as a decimal.
- 3. How does your answer to Question 2 compare to your classmates' answers?
- 4. Average all of your classmates' answers to Question 2. Write the approximate ratio of circumference to the diameter as a fraction and as a decimal.

NOTES

1.3

The Circumference Formula



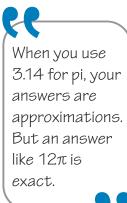
The number \mathbf{pi} (π) is the ratio of the circumference of a circle to its diameter. That is $\mathrm{pi} = \frac{\mathrm{circumference}\ \mathrm{of}\ \mathrm{a}\ \mathrm{circle}}{\mathrm{diameter}\ \mathrm{of}\ \mathrm{a}\ \mathrm{circle}}$, or $\pi = \frac{C}{d}$, where C is the circumference of the circle, and d is the diameter of the circle. The number π has an infinite number of decimal digits that never repeat. Some approximations used for the value π are 3.14 and $\frac{22}{7}$.

- 1. Use this information to write a formula for the circumference of a circle, where *d* represents the diameter of a circle and *C* represents the circumference of a circle.
- 2. Rewrite the formula for the circumference of a circle, where r represents the radius of a circle and C represents the circumference of a circle.

- 3. Use different representations for π to calculate the circumference of a circle.
 - a. Calculate the circumference of a circle with a diameter of 4.5 centimeters and a circle with a radius of 6 inches. Round your answer to the nearest ten-thousandths, if necessary.

Value for π	d = 4.5 centimeters	r = 6 inches
π		
Use the π key on a calculator		
Use 3.14 for π		
Use $\frac{22}{7}$ for π		

b. Compare your circumference calculations. How do the different values of π affect your calculations?



- 4. Use the circumference of a circle formula to determine each unknown. Use 3.14 for π .
 - a. Compute the diameter of the circle with a circumference of 65.94 feet.

b. Compute the radius of the circle with a circumference of 109.9 millimeters.



5. What is the minimum amount of information needed to compute the circumference of a circle?

	TALK the TALK		
	Twice		
	Use what you have learned to compare circles by their characteristics. 1. Using your compass, draw each circle.		
	a. radius length of 3 centimeters	b. diameter length of3 centimeters	
	2. Describe the similarities an two circles.	d differences between your	
		etween the circumferences of	
	the two circles.		
	4. Describe the circumference	e-to-diameter ratio of all circles.	
	\		

Measuring the Distance Around a Circle

