Pi: The Ultimate Ratio

Exploring the Ratio of Circle Circumference to Diameter

WARM UP

Scale up or down to determine an equivalent ratio.

- 1. $\frac{18 \text{ miles}}{3 \text{ hours}} = \frac{?}{1 \text{ hour}}$
- 2. $\frac{\$750}{4 \text{ days}} = \frac{?}{1 \text{ day}}$
- 3. $\frac{12 \text{ in.}}{1 \text{ ft}} = \frac{?}{5 \text{ ft}}$
- 4. $\frac{48 \text{ oz}}{3 \text{ lb}} = \frac{?}{1 \text{ lb}}$

LEARNING GOALS

- Identify pi (π) as the ratio of the circumference of a circle to its diameter.
- Construct circles using a compass and identify various parts of circles.
- Understand the formula for the circumference of a circle, and use the formula to solve problems.

KEY TERMS

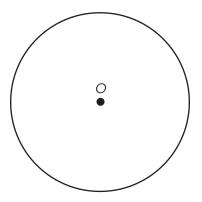
- congruent
- circle
- radius
- diameter
- circumference
- pi

You have learned about ratios. How can you use ratios to analyze the properties of geometric figures, such as circles?

Getting Started

Across and Around

A circle is shown with a point drawn at the center of the circle. The name of the point is *O*, so let's call this Circle *O*.



- Be sure to include units when you record your measurements.

- 1. Analyze the distance around the circle.
 - a. Use a string and a centimeter ruler to determine the distance around the circle.
 - b. How does your measurement compare to your classmates' measurements? Summarize the similarities and differences.
- 2. Draw a line from a point on the circle to the center of the circle, point *O*.
 - a. Measure your line using your centimeter ruler.
 - b. How does your measurement compare to your classmates' measurements? Summarize the similarities and differences.

Analyzing the Parts of a Circle

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Everyone can identify a circle when they see it, but defining a circle is a bit harder. Can you define a circle without using the word *round*? Investigating how a circle is formed will help you mathematically define a circle.

1. Follow the given steps to investigate how a circle is formed.

Step 1: In the space provided, draw a point and label the point *A*.

Step 2: Use a centimeter ruler to locate and draw a second point that is exactly 5 cm from point *A*. Label this point *B*.

Step 3: Locate a third point that is exactly 5 cm from point A. Label this point *C*.

Step 4: Repeat this process until you have drawn at least ten distinct points that are each exactly 5 cm from point A.

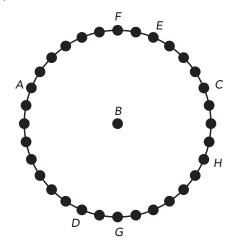
3. Define the term *circle* without using the word *round*.

2. How many other points could be located exactly 5 cm from

relation to point A?

point A? How would you describe this collection of points in

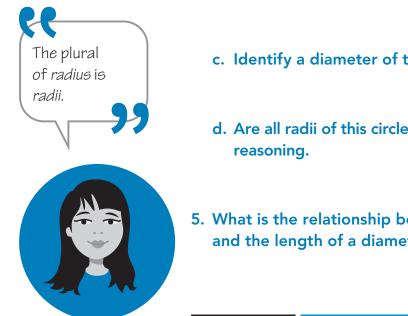
A circle is a collection of points on the same plane equidistant from the same point. The center of a circle is the point from which all points on the circle are equidistant. Circles are named by their center point.



- 4. Use the circle shown to answer each question.
 - a. Name the circle.

The **radius** of a circle is a line segment formed by connecting a point on the circle and the center of the circle. The distance across a circle through the center is the diameter of the circle. The **diameter** of a circle is a line segment formed by connecting two points on the circle such that the line segment passes through the center point. The distance around a circle is called the **circumference** of the circle.

- b. Identify a radius of the circle.
- c. Identify a diameter of the circle.
- d. Are all radii of this circle the same length? Explain your reasoning.
- 5. What is the relationship between the length of a radius and the length of a diameter?





Let's explore circles. Use circles A, B, D, E, and O provided at the end of the lesson. Circle O is the same as the circle from the activity Across and Around.

1. Use a string and a centimeter ruler to measure the distance from a point on the circle to the center and the distance around each circle. Record your measurements in the table. In the last column, write the ratio of *Circumference* : *Diameter* in fractional form.

Circle	Circumference	Radius	Diameter	<u>Circumference</u> Diameter
Circle A				
Circle B				
Circle O				
Circle D				
Circle E				

- 2. Average the ratios recorded for $\frac{\text{Circumference}}{\text{Diameter}}$. What is the approximate ratio for the circumference to the diameter for the set of circles? Write the approximate ratio as a fraction and as a decimal.
- 3. How does your answer to Question 2 compare to your classmates' answers?
- 4. Average all of your classmates' answers to Question 2. Write the approximate ratio of circumference to the diameter as a fraction and as a decimal.

1.3

NOTES



The number **pi** (π) is the ratio of the circumference of a circle to its diameter. That is pi = $\frac{\text{circumference of a circle}}{\text{diameter of a circle}}$, or $\pi = \frac{C}{d}$, where C is the circumference of the circle, and d is the diameter of the circle. The number π has an infinite number of decimal digits that never repeat. Some approximations used for the value π are 3.14 and $\frac{22}{7}$.

- Use this information to write a formula for the circumference of a circle, where d represents the diameter of a circle and C represents the circumference of a circle.
- 2. Rewrite the formula for the circumference of a circle, where *r* represents the radius of a circle and *C* represents the circumference of a circle.
- 3. Use different representations for π to calculate the circumference of a circle.
 - a. Calculate the circumference of a circle with a diameter of 4.5 centimeters and a circle with a radius of 6 inches. Round your answer to the nearest ten-thousandths, if necessary.

Value for π	d = 4.5 centimeters	r = 6 inches
π		
Use the π key on a calculator		
Use 3.14 for π		
Use $\frac{22}{7}$ for π		

b. Compare your circumference calculations. How do the different values of π affect your calculations?

- 4. Use the circumference of a circle formula to determine each unknown. Use 3.14 for π .
 - a. Compute the diameter of the circle with a circumference of 65.94 feet.

b. Compute the radius of the circle with a circumference of 109.9 millimeters.

5. What is the minimum amount of information needed to compute the circumference of a circle?

When you use 3.14 for pi, your answers are approximations. But an answer

like 12π is exact. NOTES

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Twice

Use what you have learned to compare circles by their characteristics.

- 1. Using your compass, draw each circle.
 - a. radius length of 3 centimeters
- b. diameter length of 3 centimeters

- 2. Describe the similarities and differences between your two circles.
- 3. Describe the relationship between the circumferences of the two circles.

4. Describe the circumference-to-diameter ratio of all circles.

